

## Core Maths

## Marking Scheme / Hints to Solution

## May Unit Test

Note :- Any relevant solution not mentioned here but correct would be suitably awarded

- Q1 d)  $\{\{5, 6\}\}$
- Q2 b)  $\{6, 8, 9, 10, 11, 12\}$
- Q3 b) -19
- Q4 B) none
- Q5 d) U
- Q6 c)  $\mathbb{R} - \{-1\}$
- Q7 b) 64
- Q8 a)  $\{(2,3), (2,4), (3,4), (4,6)\}$
- Q9 c) Identity function
- Q10 c)  $2^6 - 1$
- Q11 b) Domain =  $(-\infty, \infty)$  and Range =  $[0, \infty)$
- Q12 c) A is true and R is false

Q13  $(A \cap B)' = \{8, 9, 10\}' = \{5, 6, 7, 11, 12\}$

$A' \cap B' = \{5, 6, 7, 11, 12\}$

- Q14 Let  $x \in C - B$   
 $\Rightarrow x \in C$  and  $x \notin B$   
 $\Rightarrow x \in C$  and  $x \notin A$  ( $\because A \subset B$ )  
 $\Rightarrow x \in C - A$   
 $\Rightarrow C - B \subset C - A$

Q15 (i)  $R = \{(1,6), (2,7), (3,8)\}$

(ii) Domain of  $R = \{1, 2, 3\}$

(iii) Range of  $R = \{6, 7, 8\}$

False, let  $X = \{1, 2, 3\}$   
 let  $Y = \{1, 2, 3, 4\}$   
 and  $Z = \{1, 2, 3, 4, 5, 6\}$   
 Here  $X \subset Y$  and  $Y \in Z$  but  $X \notin Z$

$$f(x) = 2 - 3x, \quad x \in \mathbb{R}, \quad x > 0$$

$$\Rightarrow y = 2 - 3x$$

$$\Rightarrow 3x = 2 - y$$

$$\Rightarrow x = \frac{2-y}{3}$$

$$\text{Here } x > 0 \text{ so, } \frac{2-y}{3} > 0$$

$$\Rightarrow 2 - y > 0$$

$$\Rightarrow 2 > y$$

$$\Rightarrow y < 2$$

$$\Rightarrow y \in (-\infty, 2)$$

$$\Rightarrow \text{Range of } f(x) = (-\infty, 2)$$

$$(i) (f+g)x = f(x) + g(x) \\ = x+1 + 2x-3 \\ = 3x-2$$

$$(ii) (f-g)x = f(x) - g(x) \\ = x+1 - 2x+3 \\ = -x+4$$

$$(iii) \left(\frac{f}{g}\right)x = \frac{f(x)}{g(x)} = \frac{x+1}{2x-3} \text{ where } x \neq \frac{3}{2}$$

$$f(x) = \sqrt{x^2 - 25}$$

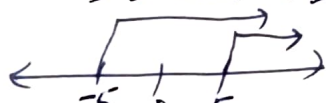
For  $f(x)$  to exist on real line

$$x^2 - 25 \geq 0$$

$$\Rightarrow (x-5)(x+5) \geq 0$$

$$x-5 \geq 0 \text{ and } x+5 \geq 0$$

$$x \geq 5 \text{ and } x \geq -5$$



$$\Rightarrow x \geq 5$$

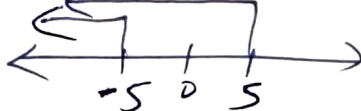
$$\Rightarrow x \in [5, \infty)$$

$\Rightarrow$

$$\Rightarrow D_f = (-\infty, -5] \cup [5, \infty)$$

$$x-5 \leq 0 \text{ and } x+5 \leq 0$$

$$x \leq 5 \text{ and } x \leq -5$$



$$\Rightarrow x \leq -5$$

$$\Rightarrow x \in (-\infty, -5]$$

$$x \in (-\infty, -5] \cup [5, \infty)$$

2 2

$\frac{1}{2}$

$\frac{1}{2}$

$\frac{1}{2}$

$\frac{1}{2}$

2

$\frac{1}{2}$

$\frac{1}{2}$

2

$\frac{1}{2}$

1+1

$\frac{1}{2}$

3

$$\Rightarrow D_f = R - (-5, 5)$$

given  $A \cap X = B \cap X = \phi$   
 $A \cup X = B \cup X$

TP  $A = B$

Proof

As  $A \cup X = B \cup X$

Take intersection with A on both sides

$$A \cap (A \cup X) = A \cap (B \cup X)$$

$$(A \cap A) \cup (A \cap X) = (A \cap B) \cup (A \cap X)$$

$$A \cup (A \cap X) = (A \cap B) \cup (A \cap X)$$

$$A \cup \phi = (A \cap B) \cup (A \cap X)$$

$$A = A \cap B$$

—(1)

1/2

Again  $A \cup X = B \cup X$

Take intersection with B on both sides

$$B \cap (A \cup X) = B \cap (B \cup X)$$

$$(B \cap A) \cup (B \cap X) = (B \cap B) \cup (B \cap X)$$

$$(B \cap A) \cup \phi = B \cup \phi$$

$$(B \cap A) = B$$

—(2)

from (1) & (2)

$$A = A \cap B = B$$

$$\Rightarrow \boxed{A = B}$$

Hence Proved.

1/2 3

Marking Scheme / Hints to Solutions  
May Unit Test

Note: - Any relevant solution not mentioned here but correct would be suitably awarded

|     |  |       |   |
|-----|--|-------|---|
| Q1  | c) -21   | 1     |   |
| Q2  | d) $2^8 - 1$   | 1     |   |
| Q3  | d) $\{x: x \in \mathbb{N}, 8 < x < 9\}$  | 1     |   |
| Q4  | d) $\{\{1, 2\}\}$ or c) $\{5, 6\}$   | 1     |   |
| Q5  | a) 16  | 1     |   |
| Q6  | c) $A = \{(2, 3), (2, 4), (3, 4), (4, 6)\}$  | 1     |   |
| Q7  | b) $\mathbb{R} - \{1\}$  | 1     |   |
| Q8  | c) Identity function   | 1     |   |
| Q9  | a) $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 12\}$   | 1     |   |
| Q10 | b) $\emptyset$   | 1     |   |
| Q11 | b) Domain = $\mathbb{R}$ and Range = $\mathbb{Z}$  | 1     |   |
| Q12 | Both are false   | 1     |   |
| Q13 | $\begin{aligned} \text{i) } (f+g)(x) &= f(x) + g(x) \\ &= 2x-3 + x+1 \\ &= 3x-2 \end{aligned}$ $\begin{aligned} \text{(ii) } (f-g)(x) &= f(x) - g(x) \\ &= 2x-3 - x-1 \\ &= x-4 \end{aligned}$ $\text{(iii) } \frac{f(x)}{g(x)} = \frac{f(x)}{g(x)} = \frac{2x-3}{x+1}, x \neq -1$ | 1 1/2 | 2 |
| Q14 | same as set A  | 1     |   |
| Q15 | $f(x) = 3-2x, x \in \mathbb{R}, x > 0$ $y = 3-2x$  | 1     |   |

$$\Rightarrow 2x = 3 - y$$

$$\Rightarrow x = \frac{3-y}{2}$$

Here  $x > 0$

$$\Rightarrow \frac{3-y}{2} > 0$$

$$\Rightarrow 3 - y > 0$$

$$\Rightarrow 3 > y$$

$$\Rightarrow y < 3$$

$$\Rightarrow y \in (-\infty, 3)$$

$$\Rightarrow R_f = (-\infty, 3)$$

(i)  $R = \{(1, 9), (2, 10), (3, 11), (4, 12)\}$

(ii) Domain of  $R = \{1, 2, 3, 4\}$

(iii) Range of  $R = \{9, 10, 11, 12\}$

Same as Q16 of set A

$$(A \cup B)' = \{5, 7, 8, 9, 10, 11, 12\}' = \{6\}$$

$$A' \cap B' = \{6\}$$

$$f(x) = \sqrt{49 - x^2}$$

For  $f(x)$  to exist on real line

$$49 - x^2 \geq 0$$

$$(7-x)(7+x) \geq 0$$

$$7-x \geq 0 \text{ and } 7+x \geq 0$$

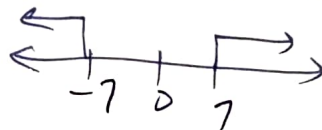
$$7 \geq x \text{ and } x \geq -7$$



$$\Rightarrow x \in [-7, 7]$$

$$7-x \leq 0 \text{ and } 7+x \leq 0$$

$$7 \leq x \text{ and } x \leq -7$$



No solution or  $\phi$

$$\Rightarrow x \in [-7, 7] \cup \phi$$

$$\Rightarrow D_f = [-7, 7]$$

02  
given  $A \cap B = A \cap C$

$$A \cup B = A \cup C$$

to  $B = C$

Proof As  $A \cup B = A \cup C$

Take intersection with  $B$  on both sides

$$B \cap (A \cup B) = B \cap (A \cup C)$$

$$\Rightarrow (B \cap A) \cup (B \cap B) = (B \cap A) \cup (B \cap C)$$

$$\Rightarrow (B \cap A) \cup B = (B \cap A) \cup (B \cap C)$$

$$\Rightarrow B = (B \cap A) \cup (B \cap C) \quad \text{--- (1)}$$

Again  $A \cup B = A \cup C$

Take intersection with  $C$  on both sides

$$\Rightarrow C \cap (A \cup B) = C \cap (A \cup C)$$

$$\Rightarrow (C \cap A) \cup (C \cap B) = (C \cap A) \cup (C \cap C)$$

$$\Rightarrow (C \cap A) \cup (C \cap B) = (C \cap A) \cup C$$

$$\Rightarrow (A \cap B) \cup (C \cap B) = C \quad \text{--- (2) } (\because A \cap B = A \cap C)$$

from (1) and (2)

$$\boxed{B = C}$$

Hence Proved

1/2

1/2



## May Test of Core Maths

Class – XI (2024-25)

Set - B

Time : 1 hour

M.M. 30

### Instructions :

- All questions are compulsory.
- This question paper has 3 Sections. Section A has 12 questions of 1 mark each.  
Section B has 6 Questions of 2 marks each. Section C has 2 questions of 3 marks each.

### Section - A

Q1 The value of  $[ -10.7 ] - [ 10.6 ]$  is ( where  $[ ]$  stands for greatest integer function)

- a) -18                      b) -19                      c) -21                      d) 0

Q2 If A is the set of the alphabets used in the word **MATHEMATICS** then the number of proper subsets of A are

- a)  $2^7$                       b)  $2^6$                       c)  $2^{11} - 1$                       d)  $2^8 - 1$

Q3 Which of the following is a null set

- a)  $\{0\}$     c)  $\{x: x + 3 = 3\}$   
b)  $\{x: x \text{ is neither positive nor negative, } x \in \mathbb{R}\}$                       d)  $\{x: x \in \mathbb{N}, 8 < x < 9\}$

Q4 Which of the following set is subset of  $A = \{\{1,2\}, 3, 4, 5, 6, 7\}$

- a)  $\{2\}$                       b)  $\{1,2\}$                       c)  $\{5,6\}$                       d)  $\{\{1, 2\}\}$

Q5 If  $P = \{2, 7\}$  and  $Q = \{4, 8\}$  then number of relations from set P to set Q are

- a) 16                      b) 64                      c) 63                      d) 45

Q6 Among these Relations given below, choose that Relation which is not Function :

- a)  $A = \{(2, 1), (3, 1)\}$     c)  $A = \{(2, 3), (2, 4), (3, 4), (4,6)\}$   
b)  $C = \{(2, 4), (3, 5), (4, 8)\}$     d)  $D = \{(3, 1), (2, 3), (4, 6)\}$

Q7 The domain of the function  $f(x) = \frac{x^2 - 8x + 12}{x^2 - 2x + 1}$  is

- a)  $\mathbb{R} - \{2, 6\}$                       b)  $\mathbb{R} - \{1\}$                       c)  $\mathbb{R} - \{-1\}$                       d)  $\mathbb{R} - \{0\}$

Q8 The domain and range are same for

- a) Constant function    c) Identity Function  
b) Signum Function    d) Greatest Integer Function

Q9 If  $U = \{1, 2, 3, \dots, 12\}$ ,  $A = \{8, 9, 10, 11\}$  and  $B = \{1, 2, 3, 4, 5, 7, 8, 9\}$

then  $(A - B)'$  is

- a)  $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 12\}$                       b)  $\{6, 8, 9, 10, 11, 12\}$                       c)  $\{1, 4, 7, 8\}$                       d)  $\emptyset$

Q10  $A \cap A' =$  \_\_\_\_\_

- a) A                      b)  $\emptyset$                       c)  $A'$                       d) U

Q11 The domain and range of  $f(x) = [x]$  is

- a) Domain =  $\mathbb{R}$  and Range =  $\mathbb{R}$
- b) Domain =  $\mathbb{R}$  and Range =  $\mathbb{Z}$
- c) Domain =  $(0, \infty)$  and Range =  $(-\infty, \infty)$
- d) Domain =  $\mathbb{R}$  and Range =  $\{0, \infty\}$

Choose according to these options in Q 12

- a) Both A and R are true and R is the correct explanation of A.
- b) Both A and R are true and R is not the correct explanation of A.
- c) A is true and R is false.
- d) A is false and R is true.

Q12 **Assertion(A)** : Let  $A = \{1, 2, 3\}$  and  $B = \{3, 4, 5\}$  then number of relations from A to B are 16

**Reason (R)** : If  $n(A) = p$  and  $n(B) = q$  then number of relations from A to B are  $p \times q$

### Section – B

Q13 Let  $f, g: \mathbb{R} \rightarrow \mathbb{R}$  be defined, respectively by  $g(x) = x + 1$ ,  $f(x) = 2x - 3$ . Find  $f + g$ ,  $f - g$ ,  $\frac{f}{g}$

Q 14 Show that if  $A \subset B$ , then  $C - B \subset C - A$

Q15 Find the range of the function:  $f(x) = 3 - 2x$ ,  $x \in \mathbb{R}$ ,  $x > 0$

Q16 Define a relation R on the set of natural numbers N by

$$R = \{ (x, y) : y = x + 8, x \text{ is natural number less than } 5 \text{ and } x, y \in \mathbb{N} \}$$

- i) Depict this relation in its roster form.
- ii) Write the domain of R.
- iii) Write the range of R.

Q 17 Determine whether the given statement is true or false. If it is true, prove it. If it is false, give an example. Statement: If  $X \subset Y$  and  $Y \in Z$ , then  $X \in Z$

Q18 If  $U = \{5, 6, 7, 8, 9, 10, 11, 12\}$ ,  $A = \{7, 8, 9, 10\}$  and  $B = \{5, 8, 9, 10, 11, 12\}$ .

$$\text{Verify that } (A \cup B)' = A' \cap B'$$

### Section - C

Q19 Find the domain of the function :  $f(x) = \sqrt{49 - x^2}$

Q20 Let A, B and C be sets such that  $A \cap B = A \cap C$  and  $A \cup B = A \cup C$  then show that  $B = C$ .







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2. This question paper has 3 Sections. Section A has 12 questions of 1 mark each. Section B has 6 Questions of 2 marks each. Section C has 2 questions of 3 marks each.

Section - A

Q1 Which of the following set is subset of  $A = \{1, \{2\}, 3, 4, \{5, 6\}, 7\}$

- a)  $\{2\}$                   b)  $\{1,5\}$                   c)  $\{5,6\}$                   d)  $\{\{5, 6\}\}$

Q2 If  $U = \{ 1, 2, 3, \dots, 12\}$ ,  $A = \{ 8, 9, 10, 11\}$  and  $B = \{ 1, 2, 3, 4, 5, 7, 8, 9\}$   
then  $(B - A)'$  is

- a)  $\{ 1, 2, 3, 4, 5, 7\}$                   b)  $\{ 6, 8, 9, 10, 11, 12\}$                   c)  $\{ 1, 4, 7, 8\}$                   d)  $\emptyset$

Q3 The value of  $[ -9.3 ] - [ 9.6 ]$  is        ( where  $[ \ ]$  stands for greatest integer function)

- a) -18                  b) -19                  c) -20                  d) 0

Q4 Which of the following is an empty set

- a)  $\{0\}$     c)  $\{x: x + 3 = 3\}$   
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Q5  $A \cup A' =$  \_\_\_\_\_

- a) A                  b)  $\emptyset$                   c)  $A'$                   d) U

Q6 The domain of the function  $f(x) = \frac{x^2 - 8x + 12}{x^2 + 2x + 1}$  is

- a)  $\mathbb{R} - \{2, 6\}$                           b)  $\mathbb{R} - \{ 1\}$                           c)  $\mathbb{R} - \{-1\}$                           d)  $\mathbb{R} - \{0\}$

Q7 If  $P = \{50, -51, 78\}$  and  $Q = \{45, 7, -8\}$  then number of relations from set P to set Q are

- a) 6                  b) 64                  c) 63                  d) 45

Q8 Among these Relations given below, choose that Relation which is not Function :

- a)  $A = \{(2, 3), (2, 4), (3, 4), (4,6)\}$                           c)  $B = \{(2, 1), (3, 1)\}$   
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- a)  $2^7$                   b)  $2^6$                   c)  $2^6 - 1$                   d)  $2^7 - 1$

Q11 The domain and range of  $f(x) = |x|$  is

- a) Domain =  $\mathbb{R}$  and Range =  $\mathbb{R}$
- b) Domain =  $(-\infty, \infty)$  and Range =  $[0, \infty)$
- c) Domain =  $(0, \infty)$  and Range =  $(-\infty, \infty)$
- d) Domain =  $\mathbb{R}$  and Range =  $\{0, \infty\}$

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### Section – B

Q13 If  $U = \{5, 6, 7, 8, 9, 10, 11, 12\}$ ,  $A = \{7, 8, 9, 10\}$  and  $B = \{5, 8, 9, 10, 11, 12\}$ .

Verify that  $(A \cap B)' = A' \cup B'$

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Q15 Define a relation R on the set of natural numbers N by

$R = \{(x, y) : y = x + 5, x \text{ is a natural number less than } 4 \text{ and } x, y \in \mathbb{N}\}$

- i) Depict this relation in its roster form.
- ii) Write the domain of R.
- iii) Write the range of R.

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Q17 Find the range of the function:  $f(x) = 2 - 3x$ ,  $x \in \mathbb{R}$ ,  $x > 0$

Q18 Let  $f, g: \mathbb{R} \rightarrow \mathbb{R}$  be defined, respectively by  $f(x) = x + 1$ ,  $g(x) = 2x - 3$ . Find  $f + g$ ,  $f - g$ ,  $\frac{f}{g}$

### Section - C

Q19 Find the domain of the function :  $f(x) = \sqrt{x^2 - 25}$

Q20 Let A and B be sets. If  $A \cap X = B \cap X = \emptyset$  and  $A \cup X = B \cup X$  for some set X, show that  $A = B$ .

