



OSDAV Public School, Kaithal  
Half yearly Exams (2024-25)  
Class : IX  
Subject : MATHEMATICS

SET-A

Time: 3 Hrs .

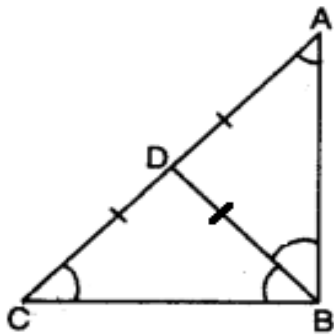
M.M. : 80

**General Instructions:-**

- I. All questions are compulsory.
- II. This Question Paper has 5 Sections A-E.
- III. Section A has 20 MCQs carrying 1 mark each
- IV. Section B has 5 questions carrying 02 marks each.
- V. Section C has 6 questions carrying 03 marks each.
- VI. Section D has 4 questions carrying 05 marks each.  
Section E has 3 case based integrated units of assessment (04 marks each) with sub-parts of the values of 1, 1 and 2 marks each respectively

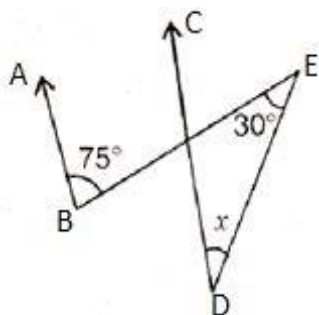
Q.N.	Questions	Marks
<b>SECTION A</b>		
1	The rational number between 7 and 8 is (a) $1/2$ (b) $11/2$ (c) $15/2$ (d) None of these	1
2	The perimeter of an equilateral triangle is 90m. The area of triangle is (a) $10\sqrt{3} \text{ m}^2$ (b) $15\sqrt{3} \text{ m}^2$ (c) $225\sqrt{3} \text{ m}^2$ (d) $100\sqrt{3} \text{ m}^2$	1
3	$x = 5, y = 2$ is a solution of the linear equation: (a) $2x + y = 14$ (b) $3x - 2y = 25$ (c) $x + 2y = 9$ (d) $x + y = 14$	1
4	Are -3 and 3 are zeroes of the polynomial $x+3$ ? (a) Only -3 is zero (b) Only 3 is zero (c) no, none is zero (d) Yes both are zeroes	1
5	A point both of whose co-ordinates are negative lies in (a) quadrant II and IV (b) quadrant I and III (c) quadrant III only (d) quadrant I only	1
6	If the x - coordinate of a point is zero, then this point lies: (a) In II quadrant (b) In I quadrant (c) On x-axis (d) On y-axis	1
7	The number 8.23232323..... is (a) a natural number (b) a whole number (c) a rational number (d) an irrational number	1
8	In two triangles ABC and DEF, $AC = DF$ , $\angle C = \angle F$ and $BC = EF$ so $\Delta ABC \cong \Delta DEF$ by which congruence rule. (a) SSS Congruence rule (b) SAS Congruence rule (c) RHS Congruence rule (d) None of these	1
9	Which of the following is a criterion for congruence of triangles? (a) SSA (b) ASA (c) ASS (d) AAA	1
10	In $\Delta PQR$ if $\angle QPR = 80$ and $PQ = PR$ , then $\angle Q$ and $\angle R$ are (a) 80, 70 (b) 80, 80 (c) 70, 80 (d) 50, 50	1
11	To solve the equation $a - 20 = 15$ which Axiom is used. (a) first (b) second (c) third (d) fourth	1
12	Write the complement of $70^\circ$ (a) $30^\circ$ (b) $20^\circ$ (c) $110^\circ$ (d) None of these	1
13	The number of Euclid Axioms is (a) 5 (b) 7 (c) 6 (d) 4	1

14	In triangle ABC, $\angle A = 100^\circ$ and $AB = AC$ Which type of triangle is this (a) Acute Angle Triangle (b) Obtuse Angle Triangle (c) Right Angle Triangle (d) None of these	1
15	Write the Coefficient of $x^2$ in the given polynomial $x^3 - 3x^2 - 5x + 8$ (a) 5 (b) 3 (c) - 3 (d) 1	1
16	Find b, if $x = 5, y = 0$ is a solution of the equation $2x + 7y = b$ (a) 8 (b) 10 (c) 15 (d) none of these	1
17	The polynomial $2x^3 - x^2 + 5x + 8$ is (a) an equation (b) a quadrinomial (c) biquadratic (d) a monomial	1
18	Let x and y be rational and irrational number respectively. Then $xy$ is necessarily (a) whole number (b) a rational number (c) an irrational number (d) a natural number	1
19	<b>Assertion:</b> The value of $95 \times 105 = 9975$ <b>Reason:</b> $(a + b)(a - b) = a^2 - b^2$ (a.) Both Assertion and Reason are correct and Reason is the correct explanation for Assertion (b.) Both Assertion and Reason are correct and Reason is not the correct explanation for Assertion. (c.) Assertion is true but the Reason is false. (d.) Assertion is false but the Reason is true.	1
20	<b>Assertion:</b> 15 is a composite number. <b>Reason :</b> 15 is an odd number. (a.) Both Assertion and Reason are correct and Reason is the correct explanation for Assertion (b.) Both Assertion and Reason are correct and Reason is not the correct explanation for Assertion. (c.) Assertion is true but the Reason is false. (d.) Assertion is false but the Reason is true.	1
<b>SECTION B</b>		
21	Write $4x = -8y + 4$ in the form of $ax + by + c = 0$ . Also write value of a, b and c.	2
22	Express $2.235235235\dots$ in form $p/q$ where p and q are integers and $q \neq 0$	2
23	Expand $(995)^3$ by suitable identity.	2
24	If Q is midpoint of line segment AB and P is midpoint of AQ then , show that $PQ = 1/4AB$	2
25	The sum of two angles of a triangle is $80^\circ$ and their difference is $20^\circ$ . Find all the angles of a triangle	2
<b>SECTION C</b>		
26	Find three solutions of equation $3x - 2y = 24$	3
27	The perimeter of triangular field is 540 m and its sides are in the ratio 12 : 17: 25. Find the area of the triangle.	3
28	Factorise $x^3 - 6x^2 + 3x + 10$	3
29	If $\frac{4+\sqrt{5}}{4-\sqrt{5}} = a + b\sqrt{5}$ . Find value of a and b .	3
30	Plots the points A(6,2) ,B(3,-5), C(0,-4), D(-2,2), E(-3,-2) and F(5,0) on the graph paper.	3
31	In a triangle ABC, D is midpoint of side AC such that $BD = \frac{1}{2}AC$ then show that $\angle ABC$ is a right angle.	3



**SECTION D**

- 32** (i) Prove that if two lines intersect at a point then the vertically opposite angles are equal.  
 (ii) In the given figure  $AB \parallel CD$ , find value of  $x$ .



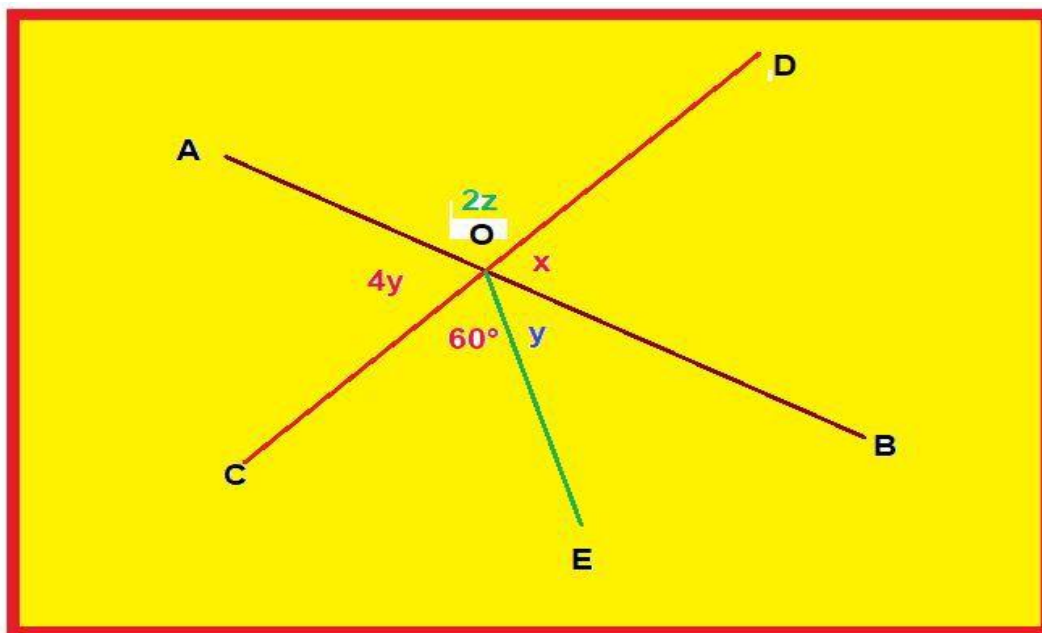
- 33** (i) Represent  $\sqrt{3}$  on the number line.  
 (ii) Simplify :  $8\sqrt{242} - 5\sqrt{50} + 3\sqrt{98}$

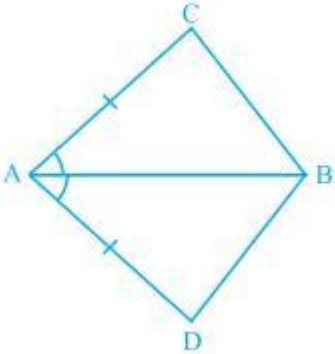
- 34** Find the value of  $a$  and  $b$  so that polynomial  $f(x) = x^3 + 10x^2 + ax + b$  is exactly divisible by  $(x - 1)$  and  $(x - 2)$ .

- 35** Find the area of a triangle whose perimeter is 360cm and its two sides are 160cm and 36cm. Calculate the altitude of triangle corresponding to its shortest side.

**SECTION E**

- 36** Maths teacher draws a straight line AB shown on the blackboard as per the following figure.



	<p>Now he told Raju to draw another line CD as in the figure  The teacher told Ajay to mark <math>\angle AOD</math> as <math>2z</math>  Suraj was told to mark <math>\angle AOC</math> as <math>4y</math>  Clive Made an angle <math>\angle COE = 60^\circ</math>  Peter marked <math>\angle BOE</math> and <math>\angle BOD</math> as <math>y</math> and <math>x</math> respectively.  Now answer the following questions on the basis of above information  (i) What is the value of <math>\angle BOE</math> ?  (ii) What is the value of <math>\angle AOD</math> ?  (iii) What is the measure of <math>x + y</math> ?</p>	
<p><b>37</b></p>	<p>Mrs Sukanya, a Maths teacher was explaining the topic of congruency of triangle by paper folding method. she took a quadrilateral shaped original sheet ACBD and folded it in a such a way from point A and B that AB bisects <math>\angle A</math> and <math>AC = AD</math></p>  <p>Now answer the following questions on the basis of above information  (i) why is <math>\angle CAB = \angle DAB</math> ?  (ii) <math>\triangle ABC</math> and <math>\triangle ABD</math> are congruent by which congruence criteria.  (iii) Show that <math>\triangle ABC \cong \triangle ABD</math></p>	<p><b>4</b></p>
<p><b>38</b></p>	<p>On 15th birthday Aryan gave party to his friends. He purchased 4 pizzas and 2 burgers from school canteen and paid Rs 800  Based on above information answer the following questions  (i) Form the linear equation in two variables.  (ii) How many solutions are possible for this equation.  (iii) Find the two solution of equation formed in part (i)</p>	<p><b>4</b></p>



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**SET-B**

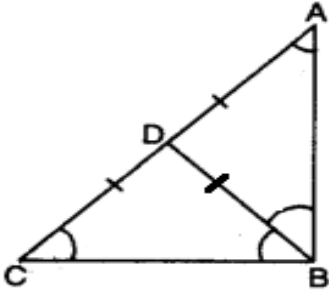
**Time: 3 Hrs.**

**M.M.: 80**

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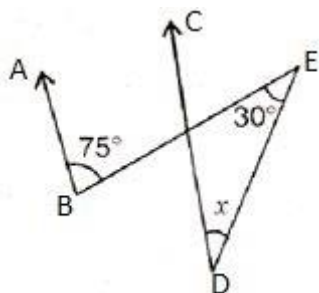
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Section **E** has 3 case based integrated units of assessment (04 marks each) with sub-parts of the values of 1, 1 and 2 marks each respectively

Q.N.	Questions	Marks
<b>SECTION A</b>		
1	The rational number between 5 and 6 is (a) $1/2$ . (b) $11/2$ (c) $5/2$ (d) None of these	1
2	The perimeter of an equilateral triangle is 60m. the area of triangle is (a) $10\sqrt{3} \text{ m}^2$ (b) $15\sqrt{3} \text{ m}^2$ (c) $20\sqrt{3} \text{ m}^2$ (d) $100\sqrt{3} \text{ m}^2$	1
3	$x = 9, y = 1$ is a solution of the linear equation: (a) $2x + y = 14$ (b) $3x - 2y = 25$ (c) $x + 2y = 14$ (d) $x + y = 14$	1
4	Are -4 and 4 are zeroes of the polynomial $x+4$ ? (a) Only -4 is zero (b) Only 4 is zero (c) no, none is zero (d) Yes both are zeroes	1
5	Which of the following is not a criterion for congruence of triangles? (a) SAS (b) ASA (c) SSA (d) SSS	1
6	If the y-coordinate of a point is zero, then this point lies: (a) In II quadrant (b) In I quadrant (c) On x-axis (d) On y-axis	1
7	The number 4.43434343..... is (a) a natural number (b) a whole number (c) a rational number (d) an irrational number	1
8	In two triangles ABC and DEF, $AC = DF, AB = DE,$ and $BC = EF$ so $\Delta ABC \cong \Delta DEF$ by which congruence rule. (a). SSS Congruence rule (b) SAS Congruence rule (c) . RHS Congruence rule (d) None of these	1
9	A point both of whose co-ordinates are Positive lies in (a) quadrant II and IV (b) quadrant I and III (c) quadrant III only (d) quadrant I only	1
10	In $\Delta PQR \angle R = \angle P$ and $QR = 4 \text{ cm}$ and $PR = 5\text{cm}$ then length of PQ is (a) 4cm (b) 2cm (c) 5cm (d) 2.5 cm	1
11	Euclid's stated that all right angles are equal to each other in the form of (a) an axiom (b) a definition (c) a postulate (d) a proof	1
12	Write the supplement of $100^\circ$ (a) $60^\circ$ (b) $80^\circ$ (c) $180^\circ$ (d) None of these	1
13	The number of Euclid postulate is (a) 5 (b) 3 (c) 6 (d) 4	1
14	The length of each side of an equilateral triangle having an area of $9\sqrt{3}\text{cm}^2$ is (a) 8cm (b) 36cm (c) 4cm (d) 6cm	1

15	Write the degree of the given polynomial $x^3 - 3x^2 - 5x + 8$ (a) 5 (b) 2 (c) 3 (d) None of the above	1
16	Find b, if $x = 5, y = 0$ is a solution of the equation $3x + 5y = b$ (a)8 (b) 10 (c)15 (d) none of these	1
17	The polynomial $2x - x^2 + 5$ is (a) an equation (b) a trinomial (c)a binomial (d) a monomial	1
18	Let x and y be rational and irrational number respectively. Then $x + y$ is necessarily (a) whole number (b) a rational number (c) an irrational number (d) a natural number	1
19	<b>Assertion:</b> The value of $98 \times 102 = 9996$ <b>Reason:</b> $(a + b)(a - b) = a^2 - b^2$ (a.) Both Assertion and Reason are correct and Reason is the correct explanation for Assertion (b.) Both Assertion and Reason are correct and Reason is not the correct explanation for Assertion. (c.) assertion is true but the reason is false. (d.) assertion is false but reason is true	1
20	<b>Assertion:</b> 33 is a composite number. <b>Reason :</b> 33 is an odd number. (a.) Both Assertion and Reason are correct and Reason is the correct explanation for Assertion (b.) Both Assertion and Reason are correct and Reason is not the correct explanation for Assertion. (c.) assertion is true but the reason is false. (d.) assertion is false but reason is true	1
<b>SECTION B</b>		
21	Write $2x = -5y - 4$ in the form of $ax + by + c = 0$ . Also write value of a, b and c.	2
22	Express $1.135135135\dots$ in form $p/q$ where p and q are integers and $q \neq 0$	2
23	Expand $(998)^3$ by suitable identity.	2
24	If a point C lies between two points A and B such that $AC = BC$ , then prove that $AC = \frac{1}{2}AB$ . Explain by drawing the figure.	2
25	In right $\Delta ABC$ right angled at A, side $AB =$ side $AC$ . Find $\angle B$ and $\angle C$	2
<b>SECTION C</b>		
26	Find three solutions of equation $2x - 3y = 18$	3
27	The perimeter of triangular field is 450 m and its sides are in the ratio 13 : 12 : 5. Find the area of the triangle.	3
28	Factorize $x^3 + 2x^2 - x - 2$	3
29	If $\frac{3+\sqrt{5}}{3-\sqrt{5}} = a + b\sqrt{5}$ . Find value of a and b .	3
30	Plots the points A(4,1), B(0,-3), C(2,-6), D(-5,5), E(-1,-2) and F(6,0) on the graph paper.	3
31	In a triangle ABC, D is midpoint of side AC such that $BD = \frac{1}{2}AC$ then show that $\angle ABC$ is a right angle. 	3

**SECTION D**

- 32** (i) Prove that if two lines intersect at a point then the vertically opposite angles are equal.  
 (ii) In the given figure  $AB \parallel CD$ , find value of  $x$ .



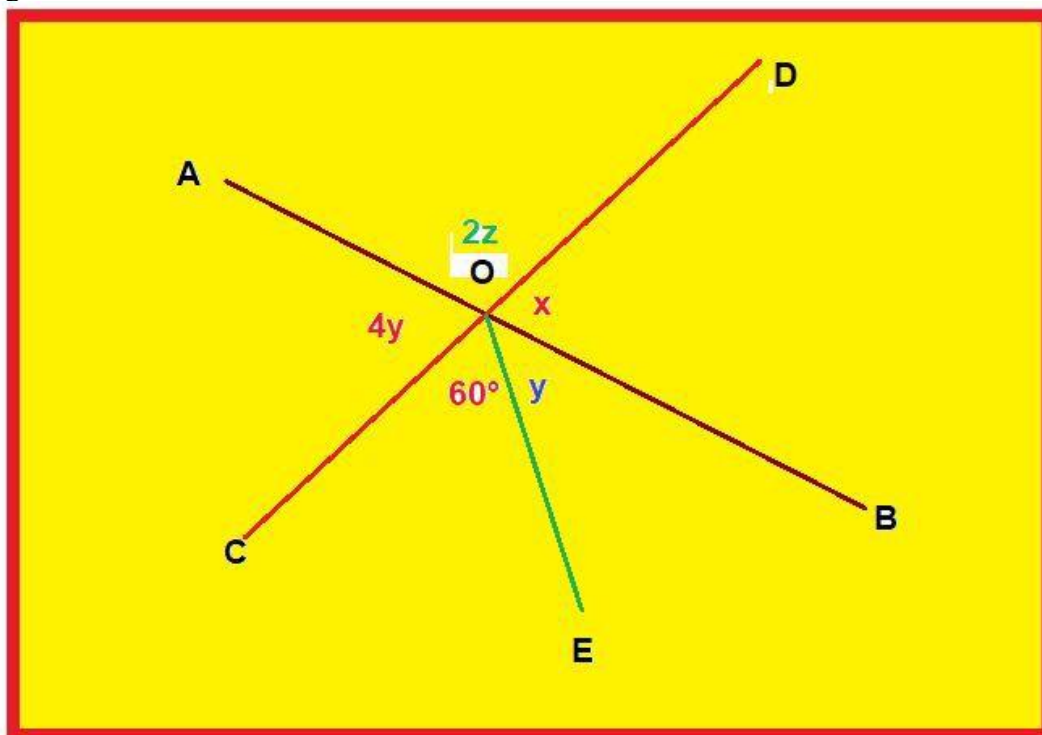
- 33** (i)  $\sqrt{\text{Represent } \sqrt{2} \text{ on the number line.}}$   
 (ii) Simplify :  $3\sqrt{45} - \sqrt{125} + \sqrt{200} - \sqrt{50}$

- 34** Find  $a$  and  $b$  so that polynomial  $f(x) = x^3 - ax^2 - 13x + b$  has  $(x - 1)$  and  $(x - 2)$  as factors.

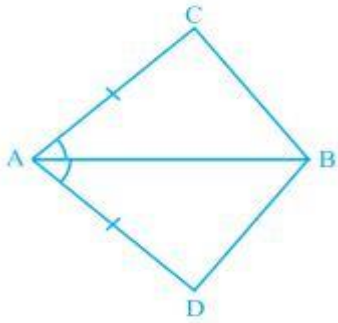
- 35** Find the area of a triangle whose perimeter is 180 cm and its two sides are 80 cm and 18 cm. Calculate the altitude of triangle corresponding to its shortest side.

**SECTION E**

- 36** Maths teacher draws a straight line AB shown on the blackboard as per the following figure.



Now he told Raju to draw another line CD as in the figure  
 The teacher told Ajay to mark  $\angle AOD$  as  $2z$   
 Suraj was told to mark  $\angle AOC$  as  $4y$   
 Clive Made an angle  $\angle COE = 60^\circ$   
 Peter marked  $\angle BOE$  and  $\angle BOD$  as  $y$  and  $x$  respectively.  
 Now answer the following questions on the basis of above information  
 (i) What is the value of  $\angle BOD$ ?  
 (ii) Find the value of  $\angle BOA$   
 (iii) What is the measure of  $\angle AOE$  ?

<p><b>37</b></p>	<p>Mrs Sukanya, a Maths teacher was explaining the topic of congruency of triangle by paper folding method. she took a quadrilateral shaped original sheet ACBD and folded it in a such a way from point A and B that AB bisects angle A and <math>AC = AD</math></p> <div style="text-align: center;">  </div> <p>Now answer the following questions on the basis of above information</p> <p>(i). why is <math>\angle CAB = \angle DAB</math>?</p> <p>(ii) <math>\triangle ABC</math> and <math>\triangle ABD</math> are congruent by which congruence criteria.</p> <p>(iii) Show that <math>\triangle ABC \cong \triangle ABD</math></p>	<p><b>4</b></p>
<p><b>38</b></p>	<p>On 15th birthday Rahul gave party to his friends. He purchased 2 pizzas and 4 burgers from school canteen and paid Rs 1000.</p> <p>Based on above information answer the following questions.</p> <p>(i) Form the linear equation in two variables.</p> <p>(ii) How many solutions are possible for this equation.</p> <p>(iii) Find the two solution of equation formed in part (i)</p>	<p><b>4</b></p>





Time: 3 Hrs .

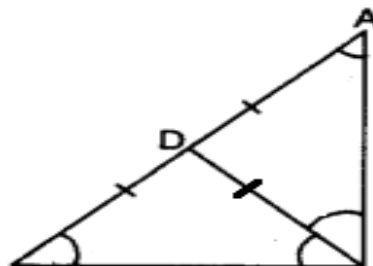
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 Section E has 3 case based integrated units of assessment (04 marks each) with sub-parts of the values of 1, 1 and 2 marks each respectively

Q.N.	Questions	Marks
SECTION A		
1	(c) $15/2$	1
2	(c) $225\sqrt{3} \text{ m}^2$	1
3	(c) $x + 2y = 9$	1
4	(a) Only -3 is zero	1
5	(c) quadrant III only	1
6	(d) On y-axis	1
7	(c) a rational number	1
8	(b) SAS Congruence rule	1
9	(b) ASA	1
10	(d) 50,50	1
11	(b) second	1
12	(b) $20^\circ$	1
13	(b) 7	1
14	(b) Obtuse Angle Triangle	1
15	(c) - 3	1
16	(b) 10	1
17	(b) a quadrinomial	1
18	(c) an irrational number/ (b) rational number	1
19	(a.) Both Assertion and Reason are correct and Reason is the correct explanation for Assertion.	1
20	(b.) Both Assertion and Reason are correct and Reason is not the correct explanation for Assertion.	1
SECTION B		
21	Write $4x = - 8y + 4$ in the form of $ax+by+c=0$ $4x + 8y - 4 = 0.$ $a = 4, b = 8$ and $c = -4$	$\frac{1}{2}$ $\frac{1}{2} \times 3$
22	Express $2.235235235\dots$ in form $p/q$ where $p$ and $q$ are integers and $q \neq 0$ Let $x = 2.235235235\dots$ eq.1 $1000x = 2235.235235\dots$ eq2 Subtracting eq.1 from eq. 2, we get $x = 2233/999$	1 1
23	Expand $(995)^3$ by suitable identity. $(1000 - 5)^3$ $= (1000)^3 - 5^3 - 3.1000.5(1000 - 5)$	$\frac{1}{2}$ 1

	= 985074875	½
24	<p>If Q is midpoint of line segment AB and P is midpoint of AQ then ,  show that <math>PQ = 1/4AB</math>  <math>AQ = 1/2AB</math> (because Q is mid point of AB)  <math>AP = 1/2AQ</math> (because P is mid point of AQ)  As <math>QB=AQ</math>  Adding AQ on both sides  <math>QB+AQ=AQ+AQ</math> (Equals are added to equals then wholes are equal)  <math>AB = 2AQ</math>  <math>AB=2(2PQ)</math>  <math>AB= 4PQ</math>  <math>1/4AB=PQ</math></p>	<p>½  ½  1</p>
25	<p>The sum of two angles of a triangle is <math>80^\circ</math> and their difference is <math>20^\circ</math>. Find all the angles of a triangle  Let angles of triangle are A, B, C  <math>A + B = 80^\circ</math> .....eq.1  <math>A - B = 20^\circ</math> .....eq.2  <math>A + B + C = 180^\circ</math> (by angle sum property of triangle )  Solving eq. 1 and eq. 2  <math>A = 50^\circ</math> , <math>B = 30^\circ</math> and <math>C = 100^\circ</math></p>	<p>½  ½ x3</p>
SECTION C		
26	<p>Find three solutions of equation <math>3x - 2y = 24</math>  1 mark for each right solution.</p>	1x3
27	<p>The perimeter of triangular field is 540 m and its sides are in the ratio 12 : 17: 25. Find the area of the triangle.  <math>12x + 17x + 25x = 540</math>  <math>54x = 540</math>  <math>x = 10</math>  sides are 120, 170 ,250  semiperimeter=<math>540 \div 2 = 270</math>  Area = <math>\sqrt{s(s - a)(s - b)(s - c)}</math>  <math>= \sqrt{270(270 - 120)(270 - 170)(270 - 250)}</math>  <math>= \sqrt{270 \times 150 \times 100 \times 20}</math>  <math>= 9000 \text{ cm}^2</math></p>	<p>1 ½  ½  1</p>
28	<p>Factorise <math>x^3 - 6x^2 + 3x + 10</math>  Factors of constant term are <math>\pm 1, \pm 2, \pm 4, \pm 5, \pm 10</math>  Put <math>x = -1</math> in the polynomial  Rem. = 0 so <math>(x + 1)</math> is the factor of given polynomial  <math>x^3 - 6x^2 + 3x + 10 \div (x + 1) = x^2 - 7x + 10</math>  <math>x^2 - 7x + 10 = (x - 5)(x - 2)</math>  <math>x^3 - 6x^2 + 3x + 10 = (x + 1)(x - 5)(x - 2)</math></p>	<p>3  1  1  1</p>
29	<p>If <math>\frac{4+\sqrt{5}}{4-\sqrt{5}} = a + b\sqrt{5}</math>. Find value of a and b .  If <math>\frac{4+\sqrt{5}}{4-\sqrt{5}} \times \frac{4+\sqrt{5}}{4+\sqrt{5}} = \frac{16+5+8\sqrt{5}}{4^2-(\sqrt{5})^2} = \frac{21+8\sqrt{5}}{11}</math>  <math>a = 21/11</math> and <math>b = 8/11</math></p>	<p>2  1</p>
30	<p>Plots the points A(6,2), B(3,-5), C(0,-4), D(-2,2), E(-3,-2) and F(5,0) on the graph paper.  For each right plotting ½ marks</p>	<p>3  ½(6)</p>
31	<p>In a triangle ABC, D is midpoint of side AC such that <math>BD = 1/2AC</math> then show that <math>\angle ABC</math> is a right angle.  D is the midpoint of AC.  <math>AD = CD</math></p>	

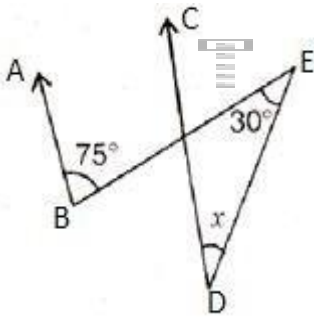


	<p> <math>BD = \frac{1}{2}AC \dots (1)</math>  <math>AC = AD + CD</math>  <math>AC = 2AD</math> or <math>2CD</math> (as <math>AD = CD</math>)            So, <math>AD = CD = \frac{1}{2}AC \dots (2)</math>            Comparing (1) and (2),  <math>AD = CD = BD \dots (3)</math>            Considering triangle DAB,            From (3), <math>AD = BD</math>            We know that the angles opposite to the equal sides are equal.  <math>\angle ABD = \angle BAD \dots (4)</math>            Considering triangle DBC,            From (3), <math>BD = CD</math>            We know that the angles opposite to the equal sides are equal.  <math>\angle BCD = \angle CBD \dots (5)</math>            Considering triangle ABC,            By angle sum property,  <math>\angle ABD + \angle DBC + \angle BAC + \angle ACB = 180^\circ</math>            As <math>\angle BAC = \angle BAD</math>            As <math>\angle ACB = \angle DCB</math>            Now, <math>2(\angle ABD + \angle DBC) = 180^\circ</math>  <math>\angle ABC = 90^\circ</math> </p>	<p>1 ½</p> <p>1 ½</p>
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SECTION D

32	<p>(i) Prove that if two lines intersect at a point then the vertically opposite angles are equal.</p> <p>           Given/To Prove            Consider ray OA that stands on the line CD            We know that the linear pair of angles is equal to 180 degrees.  <math>\angle AOC + \angle AOD = 180^\circ \dots (1)</math>            Consider ray OD that stands on the line AB  <math>\angle AOD + \angle DOB = 180^\circ \dots (2)</math>            Considering ray OB that stands on the line CD  <math>\angle DOB + \angle BOC = 180^\circ \dots (3)</math>            From (1) and (2),  <math>\angle AOC + \angle AOD = \angle AOD + \angle DOB</math>            Canceling common term,  <math>\angle AOC = \angle DOB</math>            From (2) and (3),  <math>\angle AOD + \angle DOB = \angle DOB + \angle BOC</math>            Canceling common term,  <math>\angle AOD = \angle BOC</math>            Hence proved.         </p>	<p>½</p> <p>½</p> <p>1 ½</p> <p>½</p>
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(ii) In the given figure  $AB \parallel CD$ , find value of  $x$ .

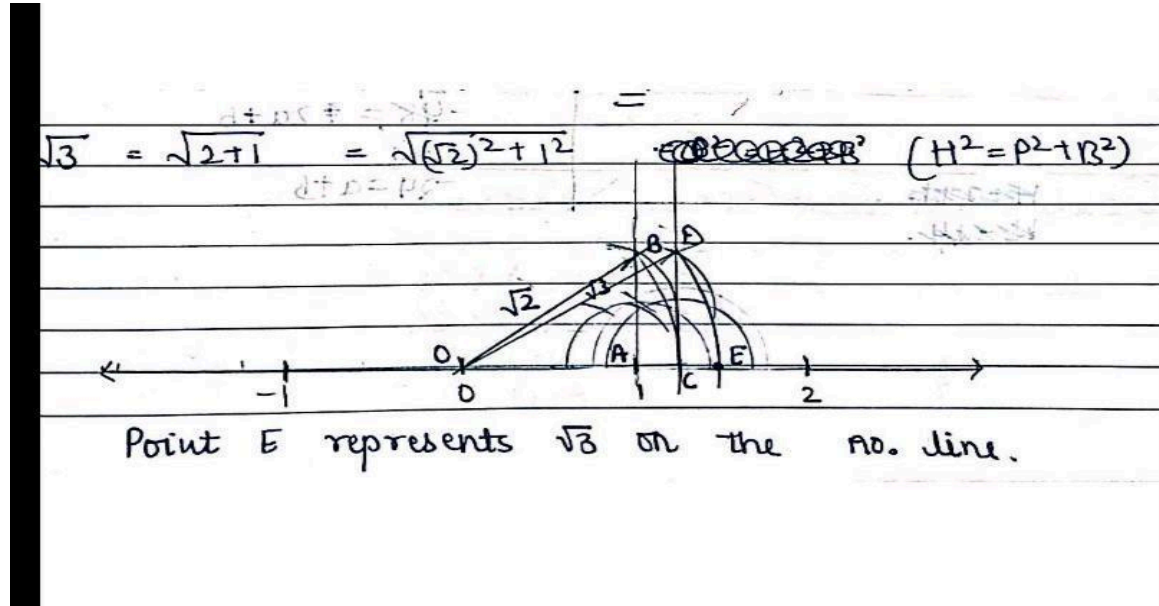


$\angle 1 = 75^\circ$  (corresponding angle)  
 $\angle 1 = x + 30^\circ$  (exterior angle property)  
 $x = 45^\circ$

1

1

33 (i) Represent  $\sqrt{3}$  on the number line.



3

(ii) Simplify:  $8\sqrt{242} - 5\sqrt{50} + 3\sqrt{98}$   
 $= 8 \times 11\sqrt{2} - 5 \times 5\sqrt{2} + 3 \times 7\sqrt{2}$   
 $= 88\sqrt{2} - 25\sqrt{2} + 21\sqrt{2} = 84\sqrt{2}$

1 ½  
 ½

34 Find the value of  $a$  and  $b$  so that polynomial  $f(x) = x^3 + 10x^2 + ax + b$  is exactly divisible by  $(x - 1)$  and  $(x - 2)$ .

$P(x) = x^3 + 10x^2 + ax + b$   
 Since  $P(x)$  is exactly divisible by  $(x - 1)$  it means that  $P(1) = 0$   
 $P(1) = 1^3 + 10 \cdot 1^2 + a \cdot 1 + b = 0$   
 $\Rightarrow 1 + 10 + a + b = 0$   
 $\Rightarrow a + b = -11$  -----(1)  
 $P(x)$  is also exactly divisible by  $(x - 2)$ ,  $P(2) = 0$   
 $P(2) = 2^3 + 10 \cdot 2^2 + 2a + b = 0$   
 $\Rightarrow 8 + 40 + 2a + b = 0$   
 $\Rightarrow 2a + b = -48$  -----(2)  
 Subtracting (1) from (2) we get  
 $2a + b - a - b = -48 - (-11)$   
 $\Rightarrow a = -37$  and  $b = +26$

1 ½

1 ½

1,1

35 Find the area of a triangle whose perimeter is 360cm and its two sides are 160cm and 36cm. Calculate the altitude of triangle corresponding to its shortest side.

Third side =  $360 - 160 - 36 = 164$ cm  
 $S = 360/2 = 180$

1

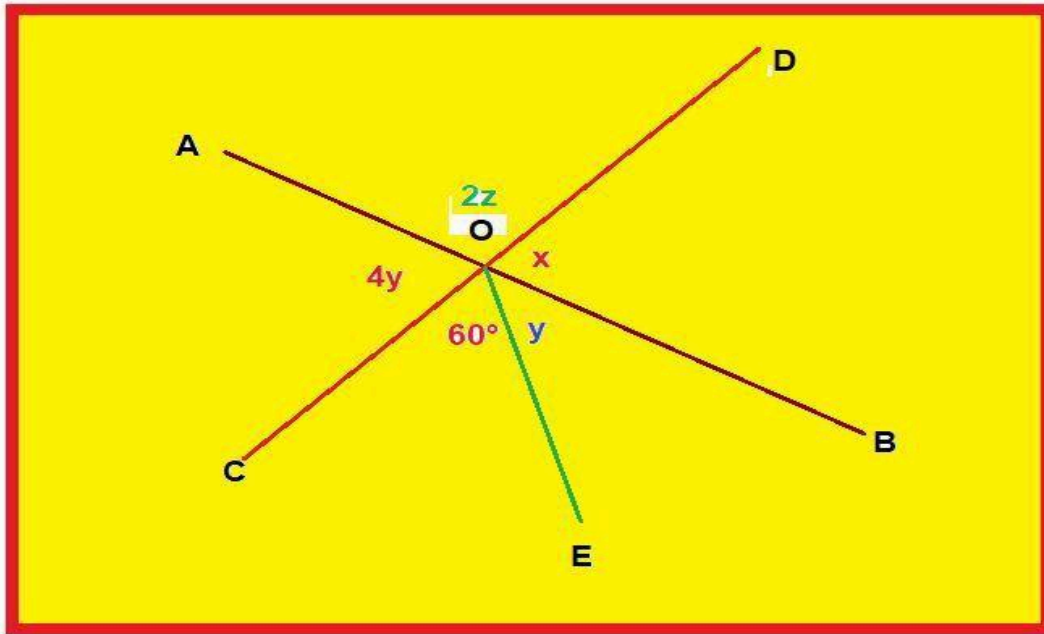
1

Area =  $2880\text{cm}^2$   
 Height =  $2 \times \text{area} / \text{base} = 2 \times 2880 / 36 = 160 \text{ cm}$

2  
1

SECTION E

36 Maths teacher draws a straight line AB shown on the blackboard as per the following figure.



Now he told Raju to draw another line CD as in the figure  
 The teacher told Ajay to mark  $\angle AOD$  as  $2z$   
 Suraj was told to mark  $\angle AOC$  as  $4y$   
 Clive Made an angle  $\angle COE = 60^\circ$   
 Peter marked  $\angle BOE$  and  $\angle BOD$  as  $y$  and  $x$  respectively.  
 Now answer the following questions on the basis of above information

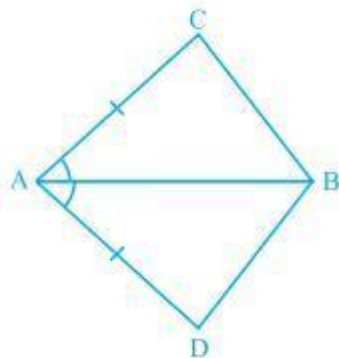
(i) What is the value of  $\angle BOE$  =  
 $4y + y + 60^\circ = 180^\circ$   
 $y = 24^\circ$

(ii) What is the value of  $\angle AOD$   
 $\angle AOD = \angle BOC$  (vertically opposite angle)  
 $\angle AOD = 84^\circ$

(iii) What is the measure of  $x + y$   
 $4y = x$   
 $x = 96^\circ$   
 $x + y = 96^\circ + 24^\circ = 120^\circ$

1  
1  
1  
1

37 Mrs Sukanya, a Maths teacher was explaining the topic of congruency of triangle by paper folding method. she took a quadrilateral shaped original sheet ACBD and folded it in a such a way from point A and B that AB bisects  $\angle A$  and  $AC = AD$



Now answer the following questions on the basis of above information

	<p>(i) why is <math>\angle CAB = \angle DAB</math> ? Because AB bisects angle A.</p> <p>(ii) <math>\triangle ABC</math> and <math>\triangle ABD</math> are congruent by which congruence criteria. By SAS congruence criteria.</p> <p>(iii) Show that <math>\triangle ABC \cong \triangle ABD</math> AC = AD (Given) <math>\angle CAB = \angle DAB</math> (AB bisect <math>\angle A</math>) AB = AB (Common) <math>\triangle ABC \cong \triangle ABD</math></p>	<p>1</p> <p>1</p> <p>2</p>
38	<p>On 15th birthday Aryan gave party to his friends. He purchased 4 pizzas and 2 burgers from school canteen and paid Rs 800</p> <p>Based on above information answer the following questions</p> <p>(i) Form the linear equation in two variables. Let cost of pizza = x Cost of burger = y <math>4x + 2y = 800</math></p> <p>(ii) How many solutions are possible for this equation. Infinite</p> <p>(iii) Find the two solutions of equation formed in part (i). One mark for each right solution.</p>	<p>1</p> <p>1</p> <p>1,1</p>



**General Instructions:-**

All questions are compulsory.

This Question Paper has 5 Sections A-E.

Section A has 20 MCQs carrying 1 mark each

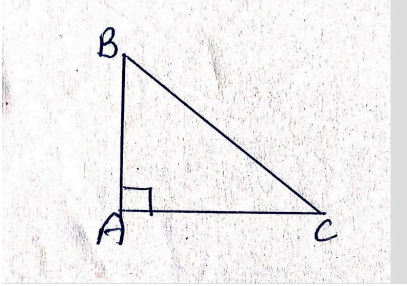
Section B has 5 questions carrying 02 marks each.

Section C has 6 questions carrying 03 marks each.

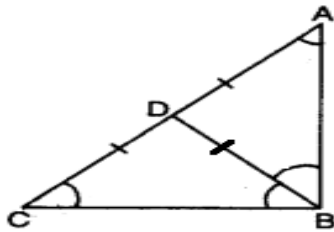
Section D has 4 questions carrying 05 marks each.

Section E has 3 case based integrated units of assessment (04 marks each) with sub-parts of the values of 1, 1 and 2 marks each respectively

Q.N.	Questions	Marks
<b>SECTION A</b>		
1	(b) $11/2$	1
2	(d) $100\sqrt{3} \text{ m}^2$	1
3	(b) $3x - 2y = 25$	1
4	(a) Only -4 is zero	1
5	(c) SSA	1
6	(c) On x-axis	1
7	(c) a rational number	1
8	(a) SSS Congruence rule	1
9	(d) quadrant I only	1
10	(a) 4cm	1
11	(c) a postulate	1
12	(b) $80^\circ$	1
13	(a) 5	1
14	(d) 6cm	1
15	(c) 3	1
16	(c)15	1
17	(b) a trinomial	1
18	(c) an irrational number	1
19	(a.) Both Assertion and Reason are correct and Reason is the correct explanation for Assertion	1
20	(b.) Both Assertion and Reason are correct and Reason is not the correct explanation for Assertion.	1
<b>SECTION B</b>		
21	Write $2x = -5y - 4$ in the form of $ax+by+c=0$ $2x + 5y + 4 = 0$ $a = 2, b = 5$ and $c = 4$	$\frac{1}{2}$ 1 $\frac{1}{2}$
22	Express $1.135135135\dots$ in form $p/q$ where $p$ and $q$ are integers and $q \neq 0$ Let $x = 1.135135135\dots$ eq.1 $1000x = 1135.135135\dots$ eq2 Subtracting eq.1 from eq. 2, we get $x = 1134/999$ $= 42/37$	$\frac{1}{2}(4)$
23	Expand $(998)^3$ by suitable identity. $= (1000 - 2)^3$ $= (1000)^3 - 2^3 - 3.1000.2(1000 - 2)$ $= 994011992$	$\frac{1}{2}$ 1 $\frac{1}{2}$
24	If a point C lies between two points A and B such that $AC = BC$ , then prove that	

	<p><math>AC = \frac{1}{2}AB</math>. Explain by drawing the figure.</p> <p><math>AC = BC</math></p> <p>Adding <math>AC</math> on both sides, we get</p> <p>According to Euclid's axioms, we know that when equals are added to equals, the wholes are equal.</p> <p><math>\Rightarrow AC + AC = BC + AC</math></p> <p><math>\Rightarrow 2 AC = AB</math></p> <p><math>\Rightarrow AC = \frac{1}{2} AB</math></p>	$\frac{1}{2}(4)$	
25	<p>In right <math>\Delta ABC</math> right angled at <math>A</math>, side <math>AB =</math> side <math>AC</math>. Find <math>\angle B</math> and <math>\angle C</math></p> <p>It is given that,</p> <p><math>AB = AC</math></p> <p><math>\therefore \angle C = \angle B</math> (Angles opposite to equal sides are also equal)</p> <p>Let <math>\angle B = \angle C = x</math></p> <p>In <math>\Delta ABC</math>,</p> <p><math>\angle A + \angle B + \angle C = 180^\circ</math> (Angle sum property of a triangle)</p> <p><math>90^\circ + x + x = 180^\circ</math></p> <p><math>90^\circ + 2x = 180^\circ</math></p> <p><math>2x = 90^\circ</math></p> <p><math>x = 45^\circ</math></p> <p><math>\therefore \angle B = \angle C = 45^\circ</math></p>		$\frac{1}{2}$ $\frac{1}{2}$ 1
<b>SECTION C</b>			
26	<p>Find three solutions of equation <math>2x - 3y = 18</math></p> <p>1 mark for each right solution.</p>	1x3	
27	<p>The perimeter of triangular field is 450 m and its sides are in the ratio 13 : 12 : 5. Find the area of the triangle.</p> <p><math>13x + 12x + 5x = 450</math></p> <p><math>30x = 450</math></p> <p><math>x = 15</math></p> <p>sides are 195,180,75</p> <p>semi perimeter= 225</p> <p>Area = <math>\sqrt{s(s-a)(s-b)(s-c)}</math></p> <p><math>= \sqrt{225(225-195)(225-180)(225-75)}</math></p> <p><math>= \sqrt{225 \times 30 \times 45 \times 150}</math></p> <p><math>= 6750 \text{ cm}^2</math></p>	$1 \frac{1}{2}$ $\frac{1}{2}$ 1	
28	<p>Factorize <math>x^3 + 2x^2 - x - 2</math></p> <p>Factors of constant term are <math>\pm 1, \pm 2, \pm 4, \pm 5, \pm 10</math></p> <p>Put <math>x = 1</math> in the polynomial</p> <p>Rem. = 0</p> <p>so <math>(x - 1)</math> is the factor of given polynomial</p> <p><math>x^3 + 2x^2 - x - 2 \div (x - 1) = x^2 + 3x + 2</math></p> <p><math>x^2 + 3x + 2 = (x + 1)(x + 2)</math></p> <p><math>x^3 + 2x^2 - x - 2</math></p> <p>Three factors are <math>(x + 1)(x - 1)(x + 2)</math></p>	1 1 1	
29	<p>If <math>\frac{3+\sqrt{5}}{3-\sqrt{5}} = a + b\sqrt{5}</math>. Find value of <math>a</math> and <math>b</math>.</p> <p>If <math>\frac{3+\sqrt{5}}{3-\sqrt{5}} \times \frac{3+\sqrt{5}}{3+\sqrt{5}} = \frac{9+5+6\sqrt{5}}{3^2-(\sqrt{5})^2} = \frac{14+6\sqrt{5}}{4}</math></p> <p><math>a = 7/2</math> and <math>b = 3/2</math></p>	2 1	
30	<p>Plots the points <math>A(4,1)</math>, <math>B(0,-3)</math>, <math>C(2,-6)</math>, <math>D(-5,5)</math>, <math>E(-1,-2)</math> and <math>F(6,0)</math> on the graph paper.</p> <p><math>\frac{1}{2}</math> mark for each right plotting.</p>	$\frac{1}{2}(6)$	
31	<p>In a triangle <math>ABC</math>, <math>D</math> is midpoint of side <math>AC</math> such that <math>BD = \frac{1}{2}AC</math> then show that <math>\angle ABC</math> is a right angle.</p> <p><math>D</math> is the midpoint of <math>AC</math>.</p>		





$$AD = CD$$

$$BD = \frac{1}{2}AC \dots (1)$$

$$AC = AD + CD$$

$$AC = 2AD \text{ or } 2CD \text{ (as } AD=CD)$$

$$\text{So, } AD = CD = \frac{1}{2} AC \dots (2)$$

Comparing (1) and (2),

$$AD = CD = BD \dots (3)$$

Considering triangle DAB,

$$\text{From (3), } AD = BD$$

We know that the angles opposite to the equal sides are equal.

$$\angle ABD = \angle BAD \dots (4)$$

Considering triangle DBC,

$$\text{From (3), } BD = CD$$

We know that the angles opposite to the equal sides are equal.

$$\angle BCD = \angle CBD \dots (5)$$

Considering triangle ABC,

By angle sum property,

$$\angle ABD + \angle DBC + \angle BAC + \angle ACB = 180^\circ$$

$$\text{As } \angle BAC = \angle BAD$$

$$\text{As } \angle ACB = \angle DCB$$

$$\text{Now, } 2(\angle ABD + \angle DBC) = 180^\circ$$

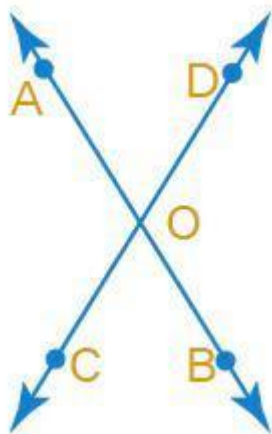
$$\angle ABC = 90^\circ$$

1 ½

1 ½

#### SECTION D

- 32 (i) Prove that if two lines intersect at a point then the vertically opposite angles are equal.



Given/To Prove

Consider ray OA that stands on the line CD

We know that the linear pair of angles is equal to 180 degrees.

$$\angle AOC + \angle AOD = 180^\circ \dots (1)$$

Consider ray OD that stands on the line AB

$$\angle AOD + \angle DOB = 180^\circ \dots (2)$$

Considering ray OB that stands on the line CD

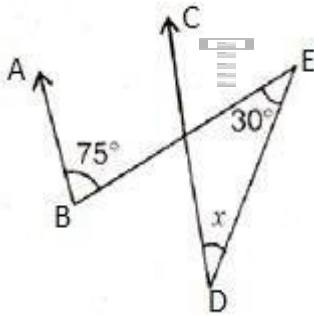
$$\angle DOB + \angle BOC = 180^\circ \dots (3)$$

½

½

From (1) and (2),  
 $\angle AOC + \angle AOD = \angle AOD + \angle DOB$   
 Canceling common term,  
 $\angle AOC = \angle DOB$   
 From (2) and (3),  
 $\angle AOD + \angle DOB = \angle DOB + \angle BOC$   
 Canceling common term,  
 $\angle AOD = \angle BOC$   
 Hence proved.

(ii) In the given figure  $AB \parallel CD$ , find value of  $x$ .



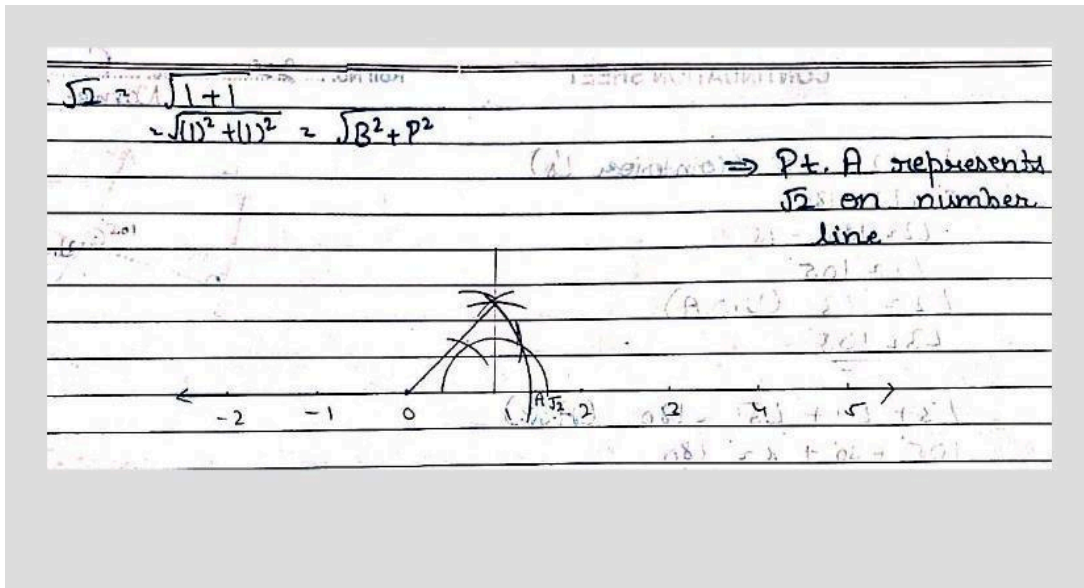
$\angle 1 = 75^\circ$  (corresponding angle)  
 $\angle 1 = x + 30^\circ$  (exterior angle property)  
 $x = 45^\circ$

1 ½

½

1  
½  
½

33 (i) Represent  $\sqrt{2}$  on the number line.



(ii) Simplify :  $3\sqrt{45} - \sqrt{125} + \sqrt{200} - \sqrt{50}$   
 $3 \times 3\sqrt{5} - 5\sqrt{5} + 10\sqrt{2} - 5\sqrt{2}$   
 $= 9\sqrt{5} - 5\sqrt{5} + 5\sqrt{2}$   
 $= 4\sqrt{5} + 5\sqrt{2}$

1  
½  
½

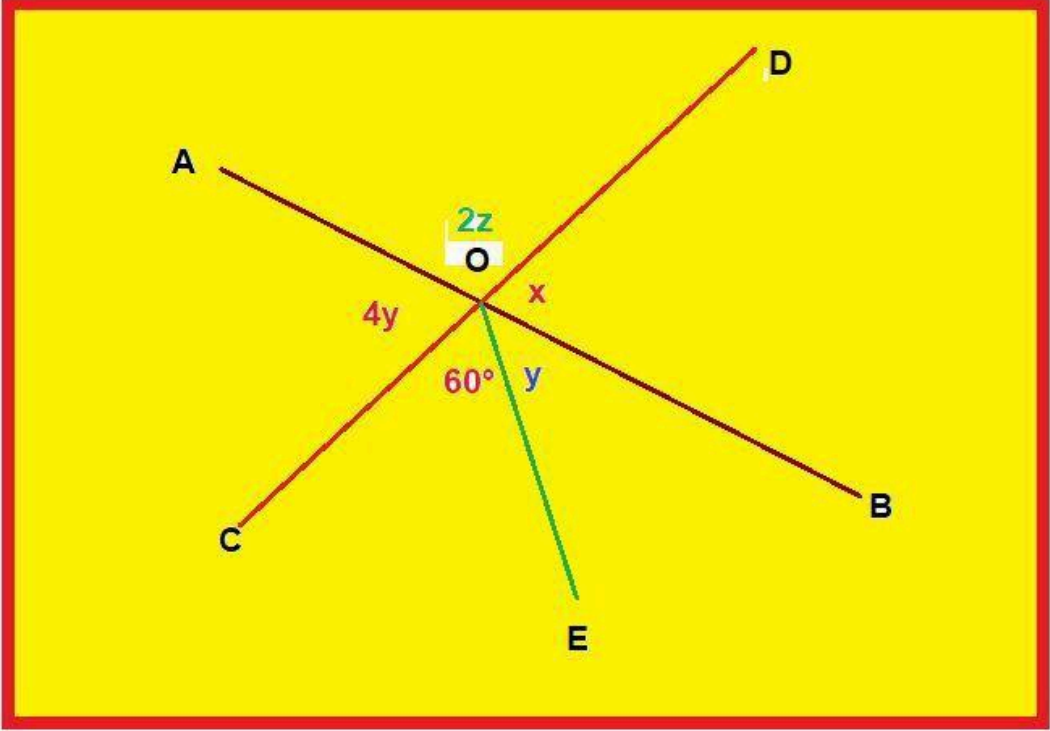
34 Find  $a$  and  $b$  so that polynomial  $f(x) = x^3 - ax^2 - 13x + b$  has  $(x - 1)$  and  $(x - 2)$  as factors.  
 Find the value of  $a$  and  $b$  so that polynomial  $f(x) = x^3 - ax^2 + 13x + b$  is exactly divisible by  $(x - 1)$  and  $(x - 2)$ .  
 $P(x) = x^3 - ax^2 - 13x + b$   
 Since  $P(x)$  is exactly divisible by  $(x - 1)$  it means that  $P(1) = 0$   
 $P(1) = 1^3 - a \cdot 1^2 - 13 \cdot 1 + b = 0$   
 $= 1 - a - 13 + b = 0$   
 $-a + b - 12 = 0$  -----(1)

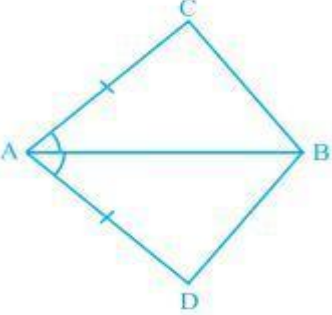
1 ½

	<p><math>P(x)</math> is also exactly divisible by <math>(x - 2)</math>, <math>P(2) = 0</math>  <math>P(2) = 2^3 - a \cdot 2^2 - 13(2) + b = 0</math>  <math>= 8 - 4a - 26 + b = 0</math>  <math>-4a + b - 18 = 0</math> -----(2)  From (1) and (2) we get  <math>\Rightarrow a = -2</math> and <math>b = 10</math></p>	<p>1 ½ 1,1</p>
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35	<p>Find the area of a triangle whose perimeter is 180 cm and its two sides are 80 cm and 18 cm. Calculate the altitude of triangle corresponding to its shortest side.  Third side = <math>180 - 80 - 18 = 82</math>cm  <math>S = 180/2 = 90</math>  Area = <math>720</math>cm<sup>2</sup>  Height = <math>2 \times \text{area} / \text{base} = 2 \times 720 / 18 = 80</math> cm</p>	<p>1 1 2 1</p>
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SECTION E

36	<p>Maths teacher draws a straight line AB shown on the blackboard as per the following figure.</p>  <p>Now he told Raju to draw another line CD as in the figure  The teacher told Ajay to mark <math>\angle AOD</math> as <math>2z</math>  Suraj was told to mark <math>\angle AOC</math> as <math>4y</math>  Clive Made an angle <math>\angle COE = 60^\circ</math>  Peter marked <math>\angle BOE</math> and <math>\angle BOD</math> as <math>y</math> and <math>x</math> respectively.  Now answer the following questions on the basis of above information</p> <p>(i) What is the value of <math>\angle BOD</math>?  <math>4y + y + 60^\circ = 180^\circ</math> (By straight angle)  <math>\angle BOD = \angle AOC = 4y = 4x \cdot 24 = 96^\circ</math></p> <p>(ii) What is the value of <math>\angle BOA</math> ?  <math>\angle BOA = 180^\circ</math></p> <p>(iii) What is the measure of <math>\angle AOE</math> ?  <math>\angle AOE = 4y + 60^\circ</math>  <math>= 96^\circ + 60^\circ</math>  <math>= 96^\circ + 60^\circ = 156^\circ</math></p>	<p>1 1 1,1</p>
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37	<p>Mrs Sukanya, a Maths teacher was explaining the topic of congruency of triangle by paper folding method. she took a quadrilateral shaped original sheet ACBD and folded it in a such a way from point A and B that AB bisects angle A and <math>AC = AD</math></p>  <p>Now answer the following questions on the basis of above information</p> <p>(i). why is <math>\angle CAB = \angle DAB</math>? Because AB bisects angle A.</p> <p>(ii) <math>\triangle ABC</math> and <math>\triangle ABD</math> are congruent by which congruence criteria. By SAS congruence criteria</p> <p>(iii) Show that <math>\triangle ABC \cong \triangle ABD</math>  <math>AC = AD</math> (Given)  <math>\angle CAB = \angle DAB</math> (AB bisect <math>\angle A</math>)  <math>AB = AB</math> (Common)  <math>\triangle ABC \cong \triangle ABD</math></p>	1 1 $\frac{1}{2}(4)$
38	<p>On 15th birthday Rahul gave party to his friends. He purchased 2 pizzas and 4 burgers from school canteen and paid Rs 1000.</p> <p>Based on above information answer the following question</p> <p>(i) Form the linear equation in two variables. Let cost of pizza =Rs. x Cost of burger = y <math>2x + 4y = 1000</math></p> <p>(ii) How many solutions are possible for this equation. infinite</p> <p>(iii) Find the two solution of equation formed in part (i)</p> <p>One mark for each right solution.</p>	1 1 1x2